Name:

This homework is due Thursday, June 22nd during recitation. If you have questions regarding any of this, feel free to ask during office hours or send me an email. When writing solutions, present your answers clearly and neatly, showing only necessary work.

1. Use the $\varepsilon-\delta$ definition of a limit to find the following;
(a) $\lim _{x \rightarrow 2} 3 x+5$

Answer:
(b) $\lim _{x \rightarrow 4} x^{2}+3 x+1$
2. Find the area of the shaded region below;

3. Evaluate the following limits:
(a) $\lim _{x \rightarrow 4} \frac{3 x-12}{x^{2}-16}$

## Answer:

(b) $\lim _{x \rightarrow 0} \frac{\sin (6 x)}{4 x}$

## Answer:

(c) $\lim _{x \rightarrow 3} \frac{\frac{1}{x}-\frac{1}{3}}{x^{2}-9}$

## Answer:

(d) $\lim _{x \rightarrow 5} \frac{\sqrt{25-x^{2}}-5}{x}$
4. Two people on bikes are 350 m apart. Person A starts riding north at a rate of $5 \mathrm{~m} / \mathrm{sec}$ and 7 minutes later Person B starts riding south at $3 \mathrm{~m} / \mathrm{sec}$. At what rate is the distance separating the two people changing 25 minutes after Person A starts riding?

## Answer:

5. Find the maximal volume of the cone that can be inscribed inside a sphere of radius 5 cm , whose top point is the centre of the sphere.

